

## Relações de Propriedades do Material

Coefficiente de Poisson

$$\nu = - \frac{\epsilon_{\text{lat}}}{\epsilon_{\text{long}}}$$

Lei de Hooke Generalizada

$$\epsilon_x = \frac{1}{E} [\sigma_x - \nu(\sigma_y + \sigma_z)]$$

$$\epsilon_y = \frac{1}{E} [\sigma_y - \nu(\sigma_x + \sigma_z)]$$

$$\epsilon_z = \frac{1}{E} [\sigma_z - \nu(\sigma_x + \sigma_y)]$$

$$\gamma_{xy} = \frac{1}{G} \tau_{xy}, \quad \gamma_{yz} = \frac{1}{G} \tau_{yz}, \quad \gamma_{zx} = \frac{1}{G} \tau_{zx}$$

onde

$$G = \frac{E}{2(1 + \nu)}$$

Relações entre  $w$ ,  $V$ ,  $M$

$$\frac{dV}{dx} = -w(x), \quad \frac{dM}{dx} = V$$

Curva Elástica

$$\frac{1}{\rho} = \frac{M}{EI}$$

$$EI \frac{d^4 v}{dx^4} = -w(x)$$

$$EI \frac{d^3 v}{dx^3} = V(x)$$

$$EI \frac{d^2 v}{dx^2} = M(x)$$

Flambagem

Carga axial crítica

$$P_{cr} = \frac{\pi^2 EI}{(KL)^2}$$

Tensão crítica

$$\sigma_{cr} = \frac{\pi^2 E}{(KL/r)^2}, \quad r = \sqrt{I/A}$$

Fórmula da secante

$$\sigma_{\text{máx}} = \frac{P}{A} \left[ 1 + \frac{ec}{r^2} \sec \left( \frac{L}{2r} \sqrt{\frac{P}{EA}} \right) \right]$$

Métodos de Energia

Conservação de energia

$$U_e = U_i$$

Energia de deformação

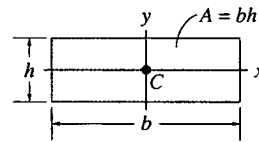
$$U_i = \frac{N^2 L}{2AE} \quad \text{carga axial constante}$$

$$U_i = \int_0^L \frac{M^2 dx}{EI} \quad \text{momento fletor}$$

$$U_i = \int_0^L \frac{f_s V^2 dx}{2GA} \quad \text{cisalhamento transversal}$$

$$U_i = \int_0^L \frac{T^2 dx}{2GJ} \quad \text{momento de torção}$$

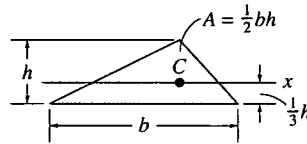
## Propriedades Geométricas dos Elementos de Área



Área retangular

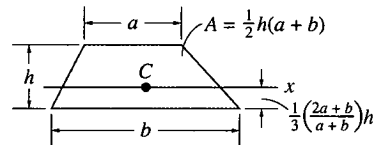
$$I_x = \frac{1}{12} bh^3$$

$$I_y = \frac{1}{12} hb^3$$

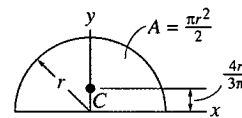


Área triangular

$$I_x = \frac{1}{36} bh^3$$



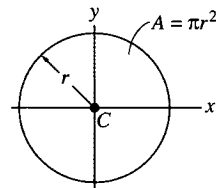
Área trapezoidal



Área semicircular

$$I_x = \frac{1}{8} \pi r^4$$

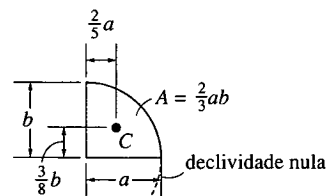
$$I_y = \frac{1}{8} \pi r^4$$



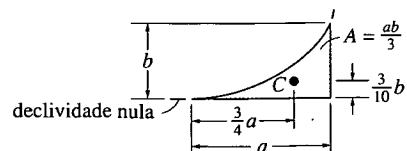
Área circular

$$I_x = \frac{1}{4} \pi r^4$$

$$I_y = \frac{1}{4} \pi r^4$$



Área semiparabólica



Área parabólica